

# Fractal Calibration for long-tailed object detection Konstantinos Panagiotis Alexandridis<sup>1</sup>, Ismail Elezi<sup>1</sup>, Jiankang Deng<sup>2</sup>, Anh Nguyen<sup>3</sup> and Shan Luo<sup>4</sup>

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#### SUMMARY

- 1. FRACAL is a space-aware logit adjustment method for imbalanced object detection;
- 2. It uses the fractal dimension to capture the occurrence patterns of classes in the training set, and fuses this information during testing via logit adjustment;
- 3. FRACAL surpasses the SOTA in long-tailed detection benchmarks and shows good performance in balanced benchmarks, without requiring training;

# MOTIVATION

In imbalanced classification, one can calibrate the logits  $z_y \in \mathbf{R}^{\mathbf{C}}$  of a model, to achieve balanced test performance. This process is called logit adjustment and it is defined as:

$$C(z_y) = z_y + \log(p_t(y)) - \log(p_s(y)),$$
 (1)

where  $p_s(y)$ ,  $p_t(y)$  are the class priors on train and test sets respectively.

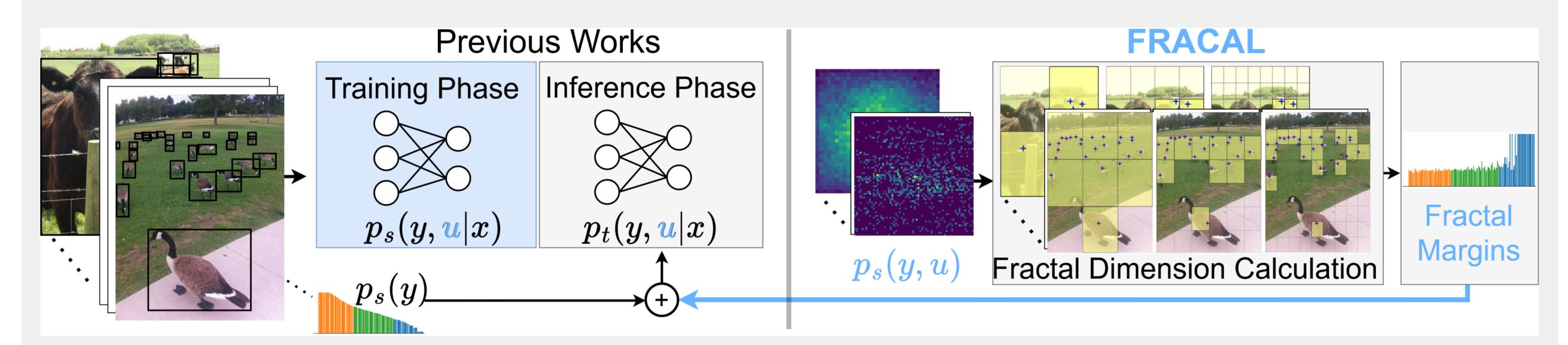


Figure 1: FRACAL embeds space-aware class information in the classification logits.

Eq.1 performs well in classification, however it does not consider the class-location relationship p(y, u), which contains crucial information in object detection. To alleviate this, we propose FRACAL, a space-aware logit adjustment method, that embeds p(y, u) information during inference via the fractal dimension, as shown in Figure 1.

# PIPELINE

FRACAL is applied during inference, in the classification logits of the detector. It makes spatially balanced detections for both the frequent classes like *hat* and rare classes like *tiara*.

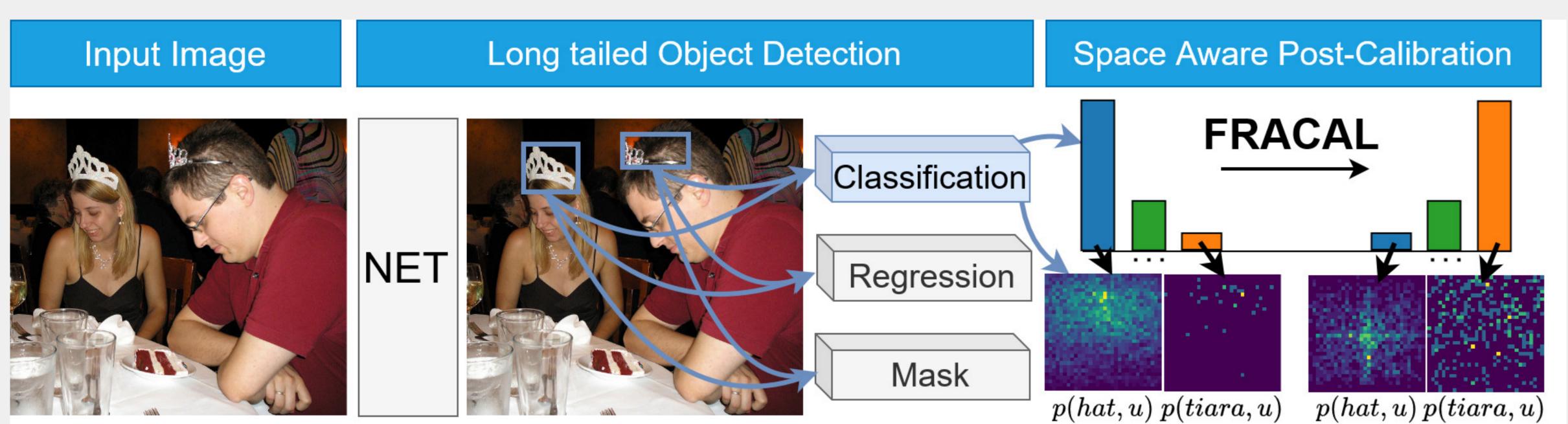


Figure 2: FRACAL pipeline.

### METHOD

To compute p(y, u) we could count the class occurrences  $n_y(\mathbf{u})$  of object locations that fall inside the cell  $\mathbf{u} = [i, j]$ , as shown below. This grid-based method, however, makes  $p(y, \mathbf{u})$  sparse and noisy, especially for large grid sizes G as shown in Figure 3-a.

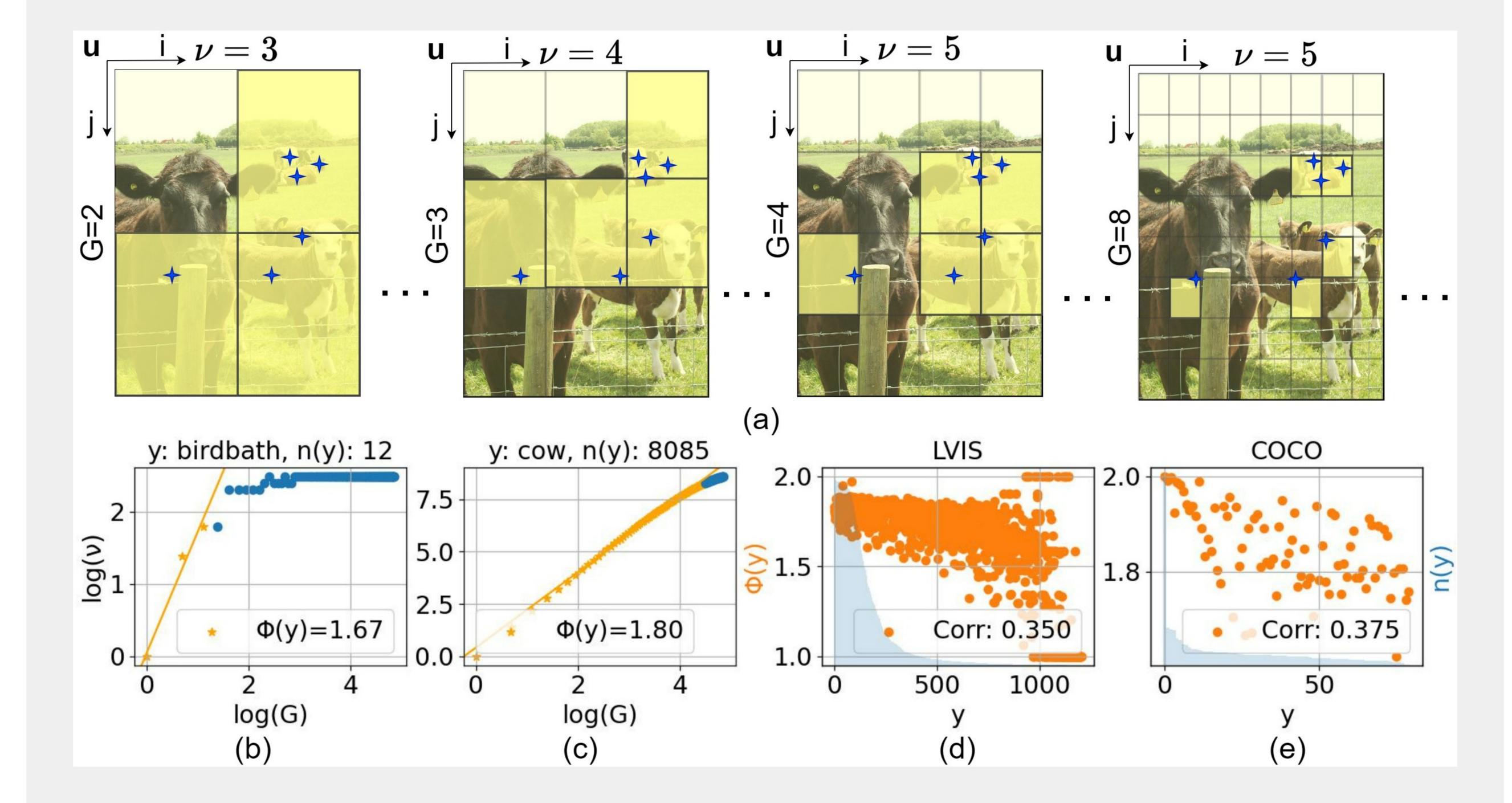


Figure 3: We iteratively count  $\nu_{\nu}$  for various grid-sizes G and do a linear interpolation to find  $\Phi$ .

To alleviate this, we propose the fractal dimension  $\Phi$ , which is a grid-independent metric and it can capture p(y, u) more robustly:

$$\Phi(y) = \lim_{G \to \infty} \frac{\log(\nu_y)}{\log(G)}, \text{ where } \nu_y = \sum_{j=0}^{G-1} \sum_{i=0}^{G-1} \mathbb{1}(n_y(\mathbf{u}))$$
(2)

To calculate Eq.2, we compute  $\nu_y - G$  pairs up to a threshold t and fit a line to these pairs as shown in Fig. 3(b) and Fig. 3(c). The slope of this line, approximates  $\Phi(y)$ . To select G we use the rule  $G \leq t = \lfloor \sqrt{n_y} \rfloor$ , which makes the calculation tractable.

We calculate  $\Phi$  for all classes in the trainset and we fuse it into the model's predictions as:

$$S(z_y) = \begin{cases} \frac{\sigma(z_y)}{\Phi(y)^{\lambda}}, & y \in \{1, ..., C\} \\ \sigma(z_y), & y = \text{background}, \end{cases}$$
 (3)

where  $\sigma()$  is the softmax function and  $\lambda$  a hyperparameter. This encourages balanced predictions and removes spatial bias. Finally, FRACAL is combined with Eq.1 as follows:

$$FRACAL(z_y) = \frac{S(C(z_y))}{\sum_{j=1}^{C+1} S(C(z_j))}.$$
(4)

#### RESULTS

Results on LVIS dataset, using ResNets, Swin and Sigmoid based detectors. FRACAL outperforms the SOTA as shown in Tables 1 (a-d).

Method	$AP^m$	Method	$AP^m$	Method	$AP^m$	Method	$\mathrm{AP}^b$
MRCNN	25.7	MRCNN	27.0	MRCNN-S	30.9	ATSS	25.3
ECM	27.4	ROG	28.8	FRACAL-S	33.6	$\mathrm{w/}\;\mathrm{FRACAL}$	26.7
LogN	27.5	LogN	29.0	MRCNN-B	36.6	$\overline{\mathrm{GFLv2}}$	27.4
FRACAL	28.6	FRACAL	29.8	FRACAL-B	38.5	$ m w/\ FRACAL$	28.9
(1-a) w/	R50	(1-b) w/	R101	(1-c) w/ $S$	Swin	(1-d) Sigmoid-	-based

Ablations using FRACAL with MaskRCNN-Resnet50. FRACAL increases the logit adjustment performance with both random samplers, in (2-a), and oversampling, in (2-b), and it outperforms the Grid based adjustment in (2-c).

$\mathbf{C}$	S	$AP^m$	$AP_r^m$		$\frac{S}{S}$	$AP^m$	$AP_r^m$	_	Method	$AP^m$	$AP_r^m$
		22.8	8.2			25.7	15.8	•	G=1	28.0	22.4
	$\checkmark$	25.6	13.7		$\checkmark$	27.7	20.7		G=2	27.1	17.5
$\checkmark$		26.3	16.5	$\checkmark$		28.0	22.4		G=4	25.0	10.5
$\checkmark$	$\checkmark$	27.3	19.0	$\checkmark$		28.6	23.0		ours	28.6	23.0
(2-a) Random Sampler			(2-b) RFS				(2-c)	Grid met	hod		

FRACAL generalises to other tasks like COCO, V3DET and OpenImages, using ResNet50.

Method	$AP^m$	$AP^{b}$	Method	$AP^{b}$	Metho	od top-1		
MRCNN	35.4	39.4	APA	29.9	CRCN	IN 65.8		
w/ FRACAL	<b>35.8</b>	39.9	w/ FRACAL	30.3	w/ FRA	CAL   67.5		
(3-a) COCO			(3-b) V3DI	ĖT	(3-c) C	(3-c) OpenImages		

FRACAL increases the fractal dimension of the distribution of the detections, in Figure 4. It reduces the calibration error and the misclassification error as shown in 4-a and 4-b respectively, however, it also increases the false positives.

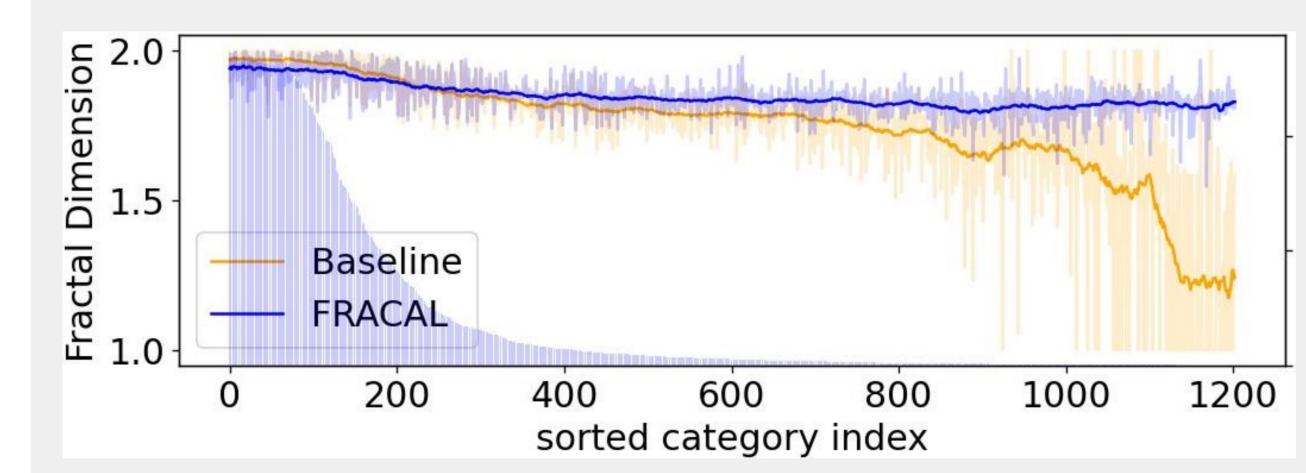


Figure 4: Φ values of class detections	•
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Method	$LaECE_0 (\downarrow)$	$LaACE_0 (\downarrow)$				
Baseline	16.8	19.8				
FRACAL (ours)	14.9	<b>15.1</b>				
(4-a) Ca	alibration Resi	alts				
Method	$dAP^b_{Cls}(\downarrow)$	$dAP^b_{Bkg}(\downarrow)$				
Baseline	31.76	6.82				
FRACAL (ours)	16.91	2.84				
(4-b) Detection Errors						

Computational cost: The weights of FRACAL need only 28 seconds to be computed, in LVIS dataset, they need to be computed only once, and they are used only during inference.

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